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J.T, PYTLINSKI AND D. SERRANO

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CENTER FOR ENERGY AND ENVIRONMENT RESEARCH

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VARIABLE GEOMETRY DARRIEUS WIND MACHINE

J.T. Pytlinski and D. Serrano

Center for Energy and Environment Research

University of Puerto Rico

## ABSTRACT

A new variable geometry Darrieus wind machine is proposed. The  
rotor attachment of the blades to the rotor can move freely up  
and down the axle allowing the blades to change shape during rota-  
tion. Experimental data for a 17m diameter Darrieus machine and  
a 2D theoretical model for multiple streamtube performance pre-  
diction were used to develop a computer simulation program for  
studying parameters that affect the machine's performance. Several  
structural and dynamic parameters were incorporated into the  
program and varied in order to simulate the machine's operation  
under a wide range of aerodynamic conditions. A parabolic  
blade was used to approximate a true airfoil shape.

The computer simulation study shows that the maximum power coefficient of a  
Darrieus turbine can not be attained by a standard turbine oper-  
ating within normally occurring rotational velocity limits.  
These results are illustrated graphically and numerically. A  
second generation variable geometry Darrieus wind turbine which

uses a telescopic blade is proposed as a potential improvement  
on the studied concept

## KEYWORDS

Wind power; vertical-axis wind turbine; Darrieus wind turbine of  
Variable geometry; theoretical analysis; computer simulation re-  
sults.

Mead and Senior Scientist, Solar Division

\*\*Graduate Student

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## INTRODUCTION

attached to the rotor at two ends. The Darrieus

gus machine was reintroduced again in the mid-1960's by research=  
EFS Of the National Research Council of Canada (NRC). "Since  
then theoretical aspects of Darrieus turbine operation have been  
studied in detail by NRC and Sandia Laboratories in the United  
States. Their research has shown that the machine has aerodyra-  
mic characteristics which in some respects differ from those of  
other wind machines; that it has a greater energy output ser

The Darrieus machine differs by several features from convention-  
al windmills which rotate about a horizontal axis. the tesbine  
which is usually composed of two or three blades, is omiaicse  
tional and accepts wind from any direction without yauning,

axle is held vertically by guy cables, the  
turbine does not need to be placed on a tower to keep the blades  
high above the ground. Moreover, the generator and gear tears  
do not need to be elevated and ate mounted on the ground. These  
features simplify the maintenance and repair of the machine cos.  
ponents.

Yet, the Darrieus wind machine is not self-starting. Its fixed-pitch blades stall at low speeds and they cannot be depended upon to drive the turbine from a standstill. To operate the Darrieus machine as self-starting, one or two Savonius rotors are mounted on the center shaft to propel the turbine at low wind speeds, or an auxiliary motor provides a starting torque. The Darrieus machines usually operate at constant revolution by being connected to a utility grid through a synchronous generator.

The Darrieus turbine uses lift as a driving force and is considerably more efficient than drag turbines such as the Savonius. It is, however, generally less efficient than propeller driven wind machines. Darrieus wind machines ranging from a few kilowatts to 250 kW are used, instead of diesel engines, to pump water and generate electric power in remote locations of Canada, the United States, Australia, New Zealand, Argentina and other countries. Research is being done to improve the aerodynamic performance of the turbine and to develop machines in the megawatt range.

#### NEW VARIABLE GEOMETRY DARRIEUS WIND TURBINE

In a standard Darrieus turbine, the tip speed ratio varies along the rotor blade from a peak near the blade mid-point to

near zero where the blade joins the torque axle. Consequently

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The ratio of the blade tip speed to wind speed.

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this ratio cannot be optimal along the entire length of the blade. The turbine geometry results from the shape imposed on blades that are permanently attached at both ends during a wide range of aerodynamic conditions and that are shaped to minimize bending stress. In a standard turbine the blade is curved like a free-spinning rope or troposkein that would allow centrifugal forces to act throughout the length of the blade. In practice however, the blades do not assume a troposkein shape. "During rotation factors imposed on the machine such as energy output per unit of mass, tip to speed ratio, aspect ratios and solidity? determine the shape of the blade during rotation. In a variable geometry turbine, however, the blades assume a shape imposed by the turbine operation conditions and by the centrifugal forces acting on the blades. In a standard turbine and in a variable geometry turbine the blades are fixed in pitch. In both, the blades have the same cross section from one end to the other. Therefore, they can be extruded and mass-produced,

Figure 1 shows a conceptual drawing of the new variable geometry Darrieus wind turbine. In this turbine the lower attachment of the blades to the rotor axle is free to move up and down,

Fig. 1. New variable geometry Darrieus wind turbine with structural spring.

ratio of the turbine height to its diameter.

The

2 the ratio of the blade area to area swept by turbine.

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The motion occurs because of variations in the turbine angular velocity caused by different wind conditions and the subsequent variation of the turbine moment of inertia, centrifugal force

under various conditions of the turbine operation, Two concepts were considered

in the first concept, the blades themselves act as a spring as shown in Fig. 1; in the second concept, an external spring is added as shown in Fig. 2.

Fig. 2. New variable geometry barrier wind turbine with external spring.

## THEORETICAL ANALYSIS

Several theories using a single streamtube, multiple streamtubes, and vortex models have been developed to evaluate the performance of a vertical axis wind turbine (Strickland, 1975, 1976; Wilson, 1976; Blackwell, 1975, 1977; Klimas, 1978, 1980; Ayaa, 1983; Paraschivoi and Belcic, 1983). The majority of these theories are based on momentum and blade element techniques and assume the turbine is enclosed in a single streamtube with uniform cross-sectional conditions or contained in a number of streamtubes, each with different conditions. Airfoil theory is usually used to determine the effective wind velocity on the blades. The theory generally used to more correctly predict changes in the power coefficient produced by different wind speeds is the multiple streamtube theory. This theory is less



?The ratio of actual power output to theoretical output.

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More complex than the vortex theory and allows for variations in blade geometry and wind shear effects. In consequence, the multiple streamtube theory (Strickland, 1975) was selected for developing a computer simulation program to study the parameters that affect the performance of a variable geometry Darrieus wind turbine.

Variable Geometry Model

The basic streamtube theory (Strickland, 1975) was adopted to analyze the performance of the new variable geometry machines shown in Figs. 1 and 2. The variable geometry model uses parabolic blades (Blackwell and Reis, 1975), as an approximation for the troposkein blades (Blackwell and Reis, 1979). Using the coordinate system in Fig. 3 and the general equation for a parabol,

$1) y = 4px^2$  end a

an expression for the radius in terms of the vertical coordinate

@ was derived:

3)

aah

Fig. 3. Rotor geometrical para

From equation (2) the blade radius for a given height can be determined. Because the angle  $\xi$  (see Fig. 3) varies with the changing geometry of the blades, this variation can be determined as well by finding the angle made by the slope of the

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blade curvature at the radine  $x$  with the horizontal Line.

Since  $\tan \xi = \frac{dx}{dr}$  the derivacive of equation (2) leads to the

expression for  $\delta$ :

:

$2^2$

seen Gee  $\$F a$

Other Parameters of the parabola such as swept area, arc length,

Moment of inertia about the axis of rotation and radius of gyration:

These have also been determined (Blackwell and Reis, 1995) and can

be listed as follows:

1. Swept area:

or  $w$

Arc length:

1

2}

B80 ee Pe ne ay

Pa : (5)

3. Moment of inertia about axis of rotation:

2,2

(san?) 5 3 3

1, = oy RA ra-3,-25.4.

a ey Ray (SE isa?" Yes? \* op

1,4

Ge + 6)

2 ea?

where:

Be

4, Radius of gyration:

2

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Each blade is treated as a parabolic beam which has one fixed end, is loaded uniformly, and whose deflection is being governed by centrifugal forces according to the following expression

(Tuma, 1965,

«)

= Young's modulus of elasticity for blade material

= cross section moment of inertia of the blade along the chord line.

\*

1

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The load on each segment along the blade chord line results from the centrifugal acceleration  $a_c$  acting on the blade end is

defined by the expression: 7

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where:

$\rho_p$  specific density of blade material

$V_g$  ? volume of blade segment

?The load can then be expressed in terms of  $F_{\perp}$  with the uniform  
dy distributed mass as follows: ©

$Y_s$

(0)

where:

$S$  = arc length of parabola

The uniformly distributed load was approximated in the computer

simulation work by using the lead acting at the radius of ays

ration

$M_p Y_e) B_p oF a_y$

You =

Both the structural spring (see Fig. 1) and the external spring  
{see Fig. 2) experience the same deflection  $\delta$  when subject? to  
the load  $W_a...$

$p_g N_y \tan(r-e8)$

oo «ay

be

where

$K_y = K_{op} + K_{op?}$  total spring constant

$K_y = K_{op}$  because & ,

=  $9 > K_{op}$

?sp

and

$K_{yq}$  7 structural spring constant

$X_{gp}$  = external spring constant

## RESULTS OF COMPUTER SIMULATION

Variable parameters such as structural and dynamic aspects of the Darrieus wind machine described above have been incorporated into the computer program to simulate the work of an Darrieus machine in a wide range of aerodynamic conditions. To determine the dynamic aspects of the machine's behavior under simulated conditions, several assumptions were made

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\* Blade is treated as beam of parabolic shape working

within the elastic limit of its material

\* Total load  $W_y$  contributes toward the blade's deflection 6



? Mechanical friction at the axle due to turbine rotation

3rd the varying geometry of the blades is negligible

\* Head resulting from the gravitational forces is negligible.

?The calculation process consists of the following steps:

1. Load on the blade is determined by using an assumed value

of the angular velocity of the turbine

2+ Deflection of blades is computed from equation (12) by

assuming different values for Key

3. New value for the turbine height is computed from:

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$f_{new}$  ? Pore

4+ A new equatorial radius,  $R$ , which corresponds to  $R_{is}$

computed by using Newton-Raphson method

5. New moment of inertia  $I$ , is computed from equation (6)

&- Power coefficient,  $C_p$ , variation with tip-to-speed ratio,

TSR, is determined by using the multiple streamtube

theory.

formance, such as solidity and tip-to-speed ratio  $Tk$ , there  
Parameters and variations of  $w$  vs  $H$ , and  $u_{ve}$   $TGk$  were  $snes$   
computed.

Computations were done for the Darrieus wind machine that has  
the following characteristics (Worstell, 1981); turbine height  
Zea B (55-8 ft), turbine diameter = 16.7 m (34.5 feet)

187 m (2014 ft), arc length = 24.1 m (79 ft), blade  
mass  $\phi$  323 kg (713 lbm), chord length  $\sim 0.533$  » (1/95' per  
blade) number of blades = 2 or 3, aerofoil section = NASR OJ1) Sy  
computer simulation program was run for the values of  $\alpha = 10^\circ$   
 $A = 20.645$  in $^2$ ,  $R = 0.3 \times 10^6$ ,  $C_y$  and  $C_p$ , taken from the values  
Of the angle of attack  $\alpha$  which was calculated according to the  
multiple streamtube theory.

The computer program was checked out by computing the variation  
of the coefficient of performance,  $C_p$ , versus tip-to-speed  
ratio. TSR, for the Darrieus wind machine having the parameters  
above. It was found that the results agreed well with those  
obtained elsewhere (Worstell, 1961) -

(36:33 ft). Such deflection is unacceptable structurally.

During the change in the machine's geometry the solidity value decreased from about 0.13 to below 0.10 which led to a decrease in the peak value of the machine's power coefficient,

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Within the rotational velocity values used (up to 69.57 rev/min), the change in turbine geometry, although large, was not sufficient to make the turbine regulate its speed by acting like a governor.

To control the Darrieus turbine geometry within acceptable blade structural limits and to dampen possible oscillations, an external spring was added as shown in Fig. 2. The computer simulation was done for different external spring constants ranging from  $K = 3000$  to  $K = 30000$ . As shown in Fig. 4 the turbine

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13.

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TSR

Fig. 4. Variation of Darrieus turbine angular velocity  $w$  (ft/s)

with tip-to-speed ratio, TSR, for spring constant  $K_S$

30000 and  $K = 70000$ ;  $N_p = 2$ ,  $c = 0.533$  m (1,75 in).

geometry is almost fixed for  $K = 30000$  and varies very little for higher values of  $K$ . The results indicate that by selecting a proper spring constant (see Figs.5 and 6) the blade deflection can be reduced to reasonable limits. The solidity variation is almost the same as for the former concept with a structural spring constant. Although the turbine responds to the variation in rev/min like a governor, as shown in Fig. 9, when replacing  $K = 30000$  by  $K = 3000$  in the computer simulation program, the machine operation parameters are even farther away from reaching governor conditions because the change in solidity is smaller than for the concept shown in Fig. 4 for the limits of  $w$  used in computations. As can be seen, the curve on

the figure changes its shape for different % values and ultimately may bend and reach a plateau at higher values of  $\sigma$  and TSR when governor operation conditions are reached.

This first generation variable geometry Darrieus wind machine led to a second generation turbine which is now being investigated. the concept allows the turbine to increase its radius by almost two-thirds of its initial value by using telescopic Blades. it is expected that the machine will respond sore

Like a governor. The use of a variable spring constant may be warranted to control the turbine geometry within @ broader range of operation parameters. The solidity will vary from 0-13 0 about 0.08 which for  $R=$  will result in & stronger  $C_y$  variation. %

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Fig. 5. Variation of bareiens turbine radive R(ft) with an~

gular velocity uo (te) for K = 3000 and KS Seonny

Ng = 2, C © 0.533 m (1.78 anj

wy

~ 65

76

38

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0

© 6 2 18 24 30 26 42 48 54 00

4

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Fig. 6. Variation of Darrieus turbine height, (ft), with angular velocity  $w$  (ft/s) for  $K = 3000$  and  $K = 300005$   
 $N_y = 2$ ,  $C = 0.533$  m (1-75 in).

Wore spreadout optimum values are ex,

pected for  $C$ , vs TSR as

shown in Fig. 8 (Strickland, 1975). °

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The variation of turbine geometry dur

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spreading out the optimum  $\phi$ , throughout

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can not self-regulate

The decrease of the solidity due to

@ Tadius causes a slight decrease in

ficient of performance and some flat=

TSR. This creates a possibility for

the variable centr:

tural and external springs.

together with other structural a

Result of this study a new genes

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range of TSR values.

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Darrieus wind machine with telescopic blades is proposed as an alternative to the fixed geometry machine.

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